

Surface hoar characteristics derived from a snow micropenetrometer using moving window statistical operations

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Abstract

This study aims to improve analytical techniques for studying stratigraphic dimensions and hardness characteristics of thin weak layers in the mountain snowpack, with particular interest to buried surface hoar layers. By determining which structural characteristics of such weak layers are associated with shear strength, we may be better able to monitor and predict stability, which is relevant for avalanche forecasting and management. We utilize moving window statistical operations to analyze SnowMicroPen (SMP) penetrometer hardness profiles of a buried surface hoar layer. Results indicate that significant weak layer thinning and hardening of the interface between the weak layer and its substratum coincided with significant increases in shear strength, as measured using a size-corrected shear strength index derived from concurrent stability tests. With aging, variations in slab thickness appeared to positively affect the hardness and inversely affect the coefficient of variation (CoV) of hardness of weak layer boundaries. These findings support previous research that proposed the strengthening of buried surface hoar layers results from the gradual penetration of the surface hoar crystals into the substratum which allows stronger bonds to form at this critical interface. These analytical techniques allow stratigraphic dimensions and hardness characteristics to be quantified and analyzed, improving our ability to monitor stratigraphic characteristics associated with shear strength and stability of the mountain snowpack.

Keywords: Snow microstructure; Snow stratigraphy; Snow hardness; Snow penetrometer; Persistent weak layer; Shear strength; Avalanches

1. Introduction

Researchers and avalanche forecasters have used a number of penetrometers over the years to analyze snow structure with the goal of better predicting avalanches (Bader et al., 1939; Bradley, 1968; Dowd and Brown, 1986; DeQuervain and Meister, 1987; Schneebeli and Johnson, 1998; Schweizer and Wiesinger, 2001; Mackenzie and Payten, 2002). Relationships between avalanche activity and generalized snowpack types derived from Ram profiles have been identified (DeQuervain and Meister, 1987) and used by avalanche forecasters (Schweizer and Wiesinger, 2001). Studies of the relationships between instabilities and thin weak layers, such as buried surface hoar, have been hindered by the spatial and force resolution of available penetrometers. With the advent of the SnowMicroPen (SMP), a high-resolution constant-speed penetrometer, hardness characteristics of thin weak layers can now be more effectively quantified (Pielmeier and Schneebeli, 2003). This instrument has been successfully implemented to delineate stratigraphic and micro-mechanical characteristics of the mountain snowpack (Johnson and Schneebeli, 1999; Schneebeli, 1999; Schneebeli et al., 1999; Pielmeier et al., 2001; Kronholm et al., 2004).

In previous SMP-related research, weak layers such as buried surface hoar have been delineated as the segment of the raw resistance signal between the upper and lower transitions (Figures 1.a and 1.d) (Birkeland et al., 2004). Using this technique, Birkeland et al. (2004) identified the micro-structural hardness of buried surface hoar layers as a potential predictor of changes in shear strength. A temporal association was identified between the shear strength and the maximum penetration resistance of the weak layer, as recorded using the SMP. It was rationalized that the increase in maximum resistance demonstrates strengthening of the strongest bonds within the weak layer, which are critical to weak layer strength. Surprisingly, no change in weak layer thickness could be identified using this delineation method (Birkeland et al., 2004).

In this study we improve SMP analysis techniques for determining the stratigraphic dimensions and hardness characteristics of buried surface hoar weak layers by incorporating two fundamental concepts. First, we expanded the scope of study to include the upper and lower transitions of the apparent weak layer (circles 1 and 2 in Figure 1.a), since these segments represent the most probable locations where strengthening occurs between surface hoar crystals and adjacent strata (Davis et al., 1996; Davis et al. 1998; Jamieson and Schweizer, 2000). In this study, the dimension containing the apparent weak layer and the adjacent transitions is referred to as the separation distance (Figure 1.e).

Second, we employ moving window statistical operations to help identify stratigraphic changes in hardness characteristics. Stratigraphic locations within and adjacent to the weak layer can be identified by analyzing trends in overlapping segments of resistance profiles. Stratigraphic delineation of thin weak layers needs to account for the size of the sensor head. This is a situation where the scale of the sample support nears the scale of the natural phenomenon (Blöschl, 1999). While the depth of each resistance reading is measured at the tip of the sensor head, the resistance signal itself results from snow structures (and void spaces) contacting the sensor head (potentially) along its entire length. The length of the sensor head is evident in the resistance signal as transitions of approximately the same length as the sensor head, entering and exiting the weak layer (circles 1 and 2 in Figure 1.a). Since the sensor head is conical, one might expect the transition force to follow a quadratic function (Figure 1.b). However, since snow is a highly heterogenous material and layer boundaries may be gradual at this scale of measurement (e.g. millimeters long), the conical relationships are likely to be obscured (gray line in Figure 1.a).

Using moving window statistical algorithms, we quantify stratigraphic dimensions and hardness variables which can then be examined for spatial and temporal patterns as well as potential associations with changes in shear strength. Since this study focused on improving our ability to analyze the SMP resistance signal and to identify potential associations with shear strength, the methodologies and results pay special attention to SMP signal processing and analysis techniques, while only briefly addressing the acquisition and analysis of the stability test data, which is extensively described by Landry et al. (2002).

2. Methods

2.1. Study Site

The study site is located in southwestern Montana at the Lionhead area, a section of the Henry's Lake Mountains approximately 15 kilometers west of West Yellowstone, Montana, U.S.A (approximately 44° 45' N; 111° 15' W). The site is sheltered from ridge-top winds and maintains a northeast-facing aspect, both characteristics that are desirable for the development and preservation of surface hoar. Slope angles range between 25-28°, allowing for gravitational effects such as creep to occur, which may play an important role in snowpack evolution and avalanche formation (Louchet, 2001). Steeper slopes were not considered for safety reasons. The study site possesses relatively uniform substrate and vegetation characteristics, primarily sub-alpine grasses, forbs, and small shrubs.

2.2. Data acquisition

In order to assess the effectiveness of our methodologies, we analyzed data previously analyzed by Birkeland et al. (2004). Field data was collected in January 2002 (Landry et al., 2002; Birkeland et al., 2004). Slope-normal hardness profiles, stability tests, and a snow profile were conducted on January 9th and 15th at two adjacent plots, defined as plot 1 and plot 2, separated by approximately 100 m. All observations were registered on a local coordinate system, such that the x- and y-axes were cross- and up-slope axes, and the z-axis was slope-normal with origin at the snow surface (Figure 2). The observations focused on monitoring the evolution of a buried surface hoar layer that had initially formed between December 21st and 26th and then was subsequently buried on December 27th. Weak layer thickness was estimated to the nearest centimeter, while the maximum surface hoar crystal size was estimated to the nearest millimeter.

Slope-normal hardness profiles were acquired using the SMP (Version 3.02). This penetrometer recorded approximately 180 resistance measurements per millimeter. The methodologies of SMP signal processing and analysis are described in the following sections.

The Quantified Loaded Column Test (QLCT) was utilized to measure *in situ* strength of the weak layer (Landry et al., 2001). Landry et al (2001) have provided a detailed description of QLCT methodologies and Birkeland and Landry (2002) and Landry et al. (2004) have described this particular dataset in detail.

Plot 1 was sampled on January 9th and contained 83 SMP profiles with a maximum sample spacing of 3 m and a minimum of 1 m (Figure 3). Thirty QLCTs were performed at three pits embedded within the SMP sampling scheme; two additional pits from plot 1 were not regarded in this study since they were not surrounded by SMP measurements. Plot 2 was sampled on January 15th and contained 128 SMP profiles with a maximum point spacing of 3 m and a minimum of 0.5 m (Figure 3). Forty-eight QLCTs were performed at five embedded pits. Although it was intended that both plots would possess the same spatial dimensions and sample sizes, mechanical difficulties hindered SMP data acquisition at plot 1. Although for an effective spatial comparison of SMP and QLCT data it would have been necessary to have QLCT tests distributed uniformly across both plots, pit-oriented tests were conducted for operational reasons and to enable pit-to-plot analysis during the original study (Landry et al., 2004).

2.3. SMP signal processing: moving window statistical operations

Using moving window statistical operations, several resistance variables, in the form of statistical profiles, were derived from the SMP measurements. The width of the moving window was equal to the length of the conical portion of the sensor head which, for this particular SMP, was 4.3 mm. This window length appeared to be a logical scale of aggregation for stratigraphic delineation and was confirmed in several trials using different window sizes. Smaller windows augmented tip interactions with individual crystals and caused stratigraphic boundaries to become less obvious while larger windows over-generalized hardness characteristics of the weak layer.

On average, each window contained approximately 790 equally weighted resistance readings. While a general mechanical or probabilistic model could account for the conical shape of the sensor tip by incorporating weighted values that increase quadratically over the length of the window, by using an equal-weights window we made no assumptions as to what part of the cone was in contact with structures at a given measurement.

The moving window spacing or offset was 0.1 mm (equal to approximately 20 measurements). Smaller offsets would have unnecessarily increased data redundancy. One-dimensional semivariance analysis on several segments of multiple SMP profiles revealed that the signal typically possessed strong autocorrelation to distances of up to 0.08 mm (0.1 mm rounded to the nearest tenth of a millimeter). In this study this dimension was considered a good estimate of the dimension at which data redundancy occurred, although this dimension can also be useful for micro-structural studies that focus on individual bond characteristics of snow types (Pielmeier and Schneebeli, 2000).

Using the above defined moving window dimensions, 9 statistical profiles were created from each SMP profile, including the minimum and maximum, the 10th-, 25th-, 50th-, 75th-, 90th-, and 98th- percentiles, and the coefficient of variation (CoV) of the resistance signal, which is the ratio of the standard deviation to the mean. The non-parametric descriptors were utilized since the SMP signal is generally non-normally distributed (skewed toward lower values with outliers at higher values). Figure 4 depicts five of the nine statistical profiles for the weak layer segment of a single SMP profile. It is important to understand that each position in a statistical profile represents a statistical value that was derived from an equal-weighted section of SMP signal the length of the sensor head.

2.4. Defining slope-normal stratigraphic positions and dimensions

The snow surface was identified in each SMP profile and was defined as the reference position (0 mm) on the slope-normal axis of the plot coordinate system (z-axis in Figure 2). Five slope-normal stratigraphic positions were defined within and adjacent to the weak layer. This was

done by locating three stratigraphic characteristics consistently evident in all of the median profiles at both plots. First, the minimum value of the median profile was defined as the center of the weak layer (Figures 4 and 5). When multiple positions within the weak layer possessed the minimum value, then their median position was defined as the center of the weak layer. Second, two adjacent maximums at the apparent boundaries with adjacent strata (i.e. where the super- and substrata begin to subside into the weak layer) were defined as the superstratum and substratum boundaries (Figures 4 and 5). Third, two additional positions were defined between the weak layer center and the apparent boundaries and are referred to as the upper and lower transitions (Figure 5).

The slope-normal dimensions of the slab and the weak layer were calculated at each SMP profile. The slab thickness was defined as the distance from the snow surface to the superstratum boundary. The separation distance, a measure related to weak layer thickness, was defined as the distance between the superstratum and substratum boundaries (Figure 5). The upper and lower segments of the separation distance were defined as the distances from the weak layer minimum to the adjacent boundaries (d' and d'' in Figure 5).

2.5. Statistical analysis

For each SMP profile, all 9 statistical profiles were sampled at the five above-defined stratigraphic positions within and adjacent to the weak layer. Hence, five sets of hardness information were generated from the statistical profiles for the five slope-normal stratigraphic positions within or adjacent to the weak layer (Figure 5).

Spatial analysis was conducted to identify, at plot 1 or plot 2, significant spatial patterns in the SMP-derived stratigraphic dimensions and hardness variables. All SMP-derived variables were tested for two components of spatial structure, including spatial trends and positive spatial autocorrelation. In addition to the description provided here, Fotheringham and Brunson (2002) and O'Sullivan and Unwin (2002) provide detailed overviews and Cressie (1993) describes spatial analysis techniques thoroughly.

For each SMP-derived variable, five trend surfaces $t(s)_{1-5}$ were calculated using five linear regressions models,

$$t(s)_1 = \alpha x + c_t$$

$$t(s)_2 = \beta y + c_t$$

$$t(s)_3 = \alpha x + \beta y + c_t$$

$$t(s)_4 = \alpha x : \beta y + c_t$$

$$t(s)_5 = \alpha x + \beta y + \alpha x : \beta y + c_t$$

whereby α , β , and c_t are regression coefficients, x and y are the cross- and up-slope SMP measurement coordinates (Figures 3), and ‘:’ signifies the relationship between x and y . For each variable, the regression model with greatest significance was chosen as the best fit trend surface model. When no significant ($p = 0.05$) trend existed for a given variable, the mean of the variable was considered its best fit trend surface model.

SMP-derived variables were then tested for positive spatial autocorrelation by conducting semivariance analysis on the residuals of the best fit trend surface models. When positive spatial autocorrelation was evident in a semivariogram (i.e. semivariance increased with lag distance, until a sill threshold value was reached) then spherical semivariogram models were fitted to empirical semivariograms using a weighted least squares function (Cressie, 1993, p. 97). The modeled semivariogram dimensions, including the range, partial sill, nugget, and nugget-sill ratio were recorded.

Classical statistical analysis was performed. Between plots 1 and 2, significant changes in SMP-derived variables were identified using the non-parametric Mann-Whitney (Wilcoxon Rank-Sum) test; boxplots were also used to graphically identify outliers and differences in central tendency. At each plot, spatially inherent relationships between slab thickness and weak layer characteristics (hardness and thickness) were tested for and quantified using simple linear regression. For this analysis, uncorrected SMP-derived variables were tested, as well as the residuals from the best fit trend surfaces. Associations between the results of this analysis and the observed change in shear strength were then rationalized.

2.6. Summary profiles of statistical profiles

Summary profiles were also calculated to visualize what the statistical profiles looked like for an entire plot. For each plot, all profiles of a given statistical descriptor were utilized to generate a median profile of the given descriptor. For example, for plot 1 a median profile of the 90th percentile profiles was calculated using all 83 of the 90th percentile statistical profiles obtained from plot 1. Summary profiles were then plotted together to visualize changes.

3. Results

3.1. Spatial analysis of stratigraphic dimensions and hardness

Spatial statistics of SMP-derived variables at plots 1 and 2 are listed in Table 1. At plot 1, very few variables possessed significant ($p < 0.05$) trend surfaces or positive spatial autocorrelation. Of the eleven significant trend surfaces at plot 1, eight describe substratum hardness characteristics (Table 1). Similarly, the lower transition and the substratum boundary possessed most of the spherical semivariance models at plot 1 (Table 1). The CoV at the substratum boundary possessed a significant ($p = 0.0019$) trend surface and pronounced positive autocorrelation. The separation distance at plot 1 also possessed both components of spatial structure.

At plot 2, all hardness variables and the CoV at all five stratigraphic positions possessed spatial structure in the form of significant trend surfaces, positive autocorrelation or, as was the case for most variables, a combination (Table 1). The majority of variables that did not possess positive spatial autocorrelation were those describing the central portion of the weak layer (Table 1). While the separation distance possessed no spatial patterns at plot 2, the slab thickness possessed both types of spatial structure (Table 1).

Between plots 1 and 2, a notable discrepancy existed between the dimensions of the semivariance models produced for hardness variables at the substratum boundary (Figure 6). For statistical descriptors apart from the first quartile statistic, the range values increased, the partial sill values decreased, and the nugget values increased (Tables 1, and Figure 6). Hence, for these hardness variables at the substratum boundary, plot 2 possessed broader spatial variations, lower plot-scale variances, and a higher inherent “noise” or stochastic character (i.e. a higher nugget-sill ratio) (Figure 6).

3.2. Significant changes in stratigraphic dimensions between plots 1 and 2

Between plots 1 and 2, the mean slope-normal separation distance decreased significantly ($p < 0.001$) from 19.0 mm to 16.7 mm, signifying a 12.1 % decrease in mean thickness while the standard deviation decreased from 2.56 mm to 2.10 mm (Table 2 and Figure 7.a). The reduction in size is evident in both the upper and lower segments of the separation distance (Table 2). Snow profile observations also indicated that the weak layer thinned markedly in the six days between plots 1 and 2, six days apart, from 2 cm to 1 cm (estimated to the nearest centimeter), and that the maximum observed crystal size decreased from 15 mm to 8 mm.

Mean slope-normal slab thickness increased significantly ($p < 0.001$) from 23.7 cm to 25.3 cm between the two plots, six days apart (Table 2 and Figure 7.b). This increase of 1.6 cm coincided with a small snow storm that occurred between observation days (see Landry (2002) for a detailed description of the snowpack development).

3.3. Significant changes in stratigraphic hardness between plots 1 and 2

Significant ($p < 0.05$) changes in the non-parametric hardness variables at all five slope-normal stratigraphic positions are summarized in Table 3 and graphically depicted in Figure 8. Figure 9 depicts the plot summaries of the non-parametric statistical profiles. Two general trends are evident in the hardness characteristics. First, a significant increase in hardness is evident at the

middle and lower stratigraphic positions in the variables describing the upper percentiles, including the 90th and 98th percentiles, and the maximum. Second, a significant decrease of hardness values occurred at the upper transition and superstratum positions, primarily in those variables describing the minimum and median hardness values. This finding corresponds with the snow profile observation: “slab softer...barely cohesive” (Landry, 2002, pp. 246). The temperature gradient through the buried surface hoar layer was 8°Cm⁻¹ on January 9th (plot 1) and 16°Cm⁻¹ on January 15th (plot 2). Approximate temperature gradients through the slab were 16.5°Cm⁻¹ and 9°Cm⁻¹, respectively.

At both plots 1 and 2, the CoV of the resistance signal was greatest at the center of the weak layer and smallest at the super- and substrata boundaries (Table 3 and Figure 10). There were significant ($p < 0.05$) increases in CoV at all five slope-normal stratigraphic positions, the least significant ($p = 0.046$) of which occurred at the weak layer position, while highly significant ($p = 0.001$) increases occurred at the remaining four positions.

3.4. Relationships between slab thickness and weak layer characteristics

Table 4 summarizes the regression results correlating slab thickness with the other SMP-derived variables. Only the results from regression tests using uncorrected values are listed, since their significance and explanatory values were slightly higher than those produced using the residuals from the best fit linear trend surfaces.

Plot 1 possessed few significant relationships, all with explanatory values less than 10 % (Table 4). However, Plot 2 possessed several highly significant ($p < 0.001$) positive correlations between slab thickness and hardness of the super- and substrata boundaries. Explanatory values were highest at the substratum boundary, ranging from 13.4 % to 33.2 %.

Significant negative correlations were identified between slab thickness and CoV of hardness at plot 1 and 2. At plot 1, a small ($R^2 = 0.054$) but significant ($p = 0.034$) inverse correlation existed between slab thickness and the CoV at the substratum boundary. At plot 2, this inverse relationship was highly significant ($p = 2 \times 10^{-9}$) and explained 25.3 % of the variation of the CoV.

In addition, at plot 2 a significant ($p = 0.017$) negative correlation existed between slab thickness and the COV of hardness.

Slab thickness also possessed significant ($p = 0.03$ and 0.0002 , respectively) positive correlations with the separation distance at both plots, explaining about 5.7% and 10.9% of the variation in the separation distance at each plot respectively.

3.5. Overview of stability test results

Classical analysis of the stability test results indicated a significant ($p = 0.001$) increase of the mean size-corrected shear strength index values from 373.5 to 522.9 between plots 1 and 2, as well as an increase in the standard deviation from 37.1 to 54.8 (Figure 7.c). Stability test results are described and interpreted in detail by Birkeland and Landry (2002), Landry (2002), and Landry et al. (2004).

4. Discussion

4.1. Spatial characteristics of stratigraphic dimensions and hardness

The absence of spatial patterns from many of the SMP-derived variables at plot 1 suggests spatial uniformity at the scale of observation (Table 1). Hence, capturing the true spatial patterns of the natural phenomenon required a different sampling scheme possessing significantly different (smaller or larger) sample spacing. At plot 1, only the substratum boundary exhibited consistent spatial patterns.

In contrast, the extensive spatial structure at plot 2 reveals that the hardness characteristics at the super- and substrata boundaries are spatially auto-correlated and the weak layer center appears uniform (Table 1). The discrepancies between semivariance models of hardness characteristics at the substratum at plot 1 and 2 reveal three potentially temporal developments: 1) local patterns in hardness became broader (increased range values), 2) the plot-scale variability decreased

(decreased partial sill values), and 3) the inherent noise increased (increased nugget) (Figure 6). Recent modeling work suggests increased nugget-sill ratios in shear strength leads to increasing slope stability (Kronholm and Birkeland, In press), so the temporal changes we observe might be a component of the slope stabilization process.

The semivariogram range for the weak layer hardness values were slightly longer than those found by Kronholm et al. (2004), but generally seem to be in agreement. An exact comparison is difficult, since Kronholm et al. (2004) excluded the weak layer's transitions and analyzed the mean of the log-transformed resistance signal.

For our results, the substrata boundary possessed consistent spatial characteristics, while large discrepancies are evident in the spatial characteristics of descriptors for other positions. For instance, the lower transition semivariogram range values at plot 2 vary from 4.5 m (for the median hardness) to 12.5 m (for the first quartile of hardness); a physical interpretation of this is difficult. The semivariograms for these variables show the spherical model (calculated using the weighted least squares function) "jumped" to a smaller range when the semivariance at short lag distances changed only slightly in the empirical variogram. This suggests using a more robust semivariogram model function would reduce the variation in the observed spatial patterns at a given stratigraphic position. Taking these limitations into account, the most important results of the spatial analysis are the general trends, the presence or absence of structure, and the typical structure(s) present at a given stratigraphic position (such as the substratum boundary).

4.2. Temporal associations between stratigraphic characteristics and weak layer strengthening

The tests for significant changes in stratigraphic dimensions and hardness characteristics of the weak layer revealed four interesting developments that coincided with the observed strengthening of the weak layer. First, the 12.1% decrease of the SMP-derived separation distance supports previous research that weak layer strengthening is accompanied by weak layer thinning (Table 2) (Davis et al., 1996; Jamieson and Schweizer, 2000). The results support the conceptual model proposed by Jamieson and Schweizer (2000) that the strengthening of buried surface layers

is in part due to surface hoar penetration of the substratum, which would cause the total layer thickness to decrease. As described by Davis et al. (1998) and Jamieson and Schweizer (2000), umbrella-like surface hoar crystals possess larger contact areas with the superstratum than with the substratum. Hence, it is likely that the upper boundary would be better preserved, while the lower boundary would penetrate into the substratum due to the overburden. Another possible cause for weak layer thinning could be a slow shear strain due to the shear stress within the weak layer, which would cause the crystals to rotate down slope from their original orientation. However, in this study no observable change in the crystal orientation was noted.

Second, the increase in hardness at the lower transition and substratum boundary coincided with the increase in shear strength, supporting previous research that identified the lower boundary of the weak layer as the critical location for strengthening (Table 3) (Davis et al., 1996; Davis et al. 1998; Jamieson and Schweizer, 2000). Evidently, despite the large temperature gradients, bond strengthening or densification occurred. This observation conforms to the conceptual model proposed by Jamieson and Schweizer (2000) that due to hoar crystal penetration into the substratum, more surface area is made available for bonding with the substratum.

Third, the decrease in hardness observed at the upper transition and superstratum boundary most likely was due to faceting in the upper portion of the snowpack (Table 3). Faceting was possible due to large temperature gradients present within the weak layer and the slab during the sampling period. The weaker resistance values imply that grain bonds became weaker or less dense, likely due to faceting. Since the shear strength didn't decrease, but actually increased between plot 1 and 2, it appears that the hardness of upper transition and the superstratum boundary did not govern changes in shear strength.

Fourth, the CoV of hardness revealed two interesting textural characteristics of the superstratum-weak layer-substratum complex. The surface hoar possessed much higher CoV values than the adjacent boundaries, since the surface hoar produced smaller mean resistance values and are highly heterogeneous. Viewed temporally, it is evident that the CoV of hardness increased, suggesting that the weak layer structure became more variable at the scale of the

moving window statistical operations (Table 3). This may have been due to the degradation of surface hoar as it aged.

4.3. Relationships between slab thickness and stratigraphic characteristics

Slab thickness appears to influence three stratigraphic characteristics (Table 4). First, the positive correlations between slab thickness and the hardness of the super- and substrata boundaries provide evidence that slab thickness positively influences the hardness of weak layer boundaries with adjacent strata. Assuming the slope-normal slab thickness is a proxy of the slope-normal load, it appears that, on a given slope at a given time, harder weak layer boundaries develop under greater loads. This relationship was stronger at plot 2 than at plot 1, suggesting that, the relationship became stronger with time, perhaps due to the small increase in overburden. Furthermore, the central portion of the weak layer was not affected by differences in slab thickness at either plot. This discrepancy is intuitive, since the boundaries of the surface hoar layer contact the adjacent strata and the central portion does not. Conversely, it would be counter-intuitive if the central portion of the surface hoar layer would become harder under greater loads (temporally or spatially) without the boundaries hardening as well.

Second, the negative correlations identified at plot 1 and 2 between slab thickness and the COV of hardness at the super- and substrata boundaries suggest that, at a given point in time, the hardness of the weak layer boundaries is less variable where the slab is thicker. Third, the weak positive relationships between slab thickness and the separation distance are counterintuitive, suggesting that at a given point in time, the weak layer was thicker where the slab was thicker. One possible cause would be that the SMP was not held perfectly perpendicular to the slope, thereby coupling thicker slab measurements with thicker weak layer measurements. The low explanatory values however show that most of the variation in slab thickness and the separation distance was not related.

4.4. Interpretation of weak layer delineation technique

The concurrence of the significant decrease in the slope-normal separation distance and the field observations between plots 1 and 2 suggests that this stratigraphic delineation technique is picking up real stratigraphic features. Interestingly, two discrepancies can be identified between these findings and the weak layer thickness results calculated by Birkeland et al. (2004). First, Birkeland et al (2004) found no significant weak layer thinning. A possible explanation for this discrepancy is differences in weak layer delineation criteria. Using manual delineation, the weak layer was defined as the segment of the resistance signal between the upper and lower transitions (excluding the transitions) (Figure 1.d). Hence, the thinning observed in our results must be occurring in the transition zones.

Second, the mean separation distances of 19.0 mm and 16.7 mm for plot 1 and 2 was markedly larger than the weak layer thickness of approximately 8 mm calculated by Birkeland et al. (2004). This discrepancy can be logically attributed to physical properties of the snowpack and the SMP geometry (Figure 1). This can be best explained if we assume a hypothetical snowpack where the super- and substrata are homogenous layers and the weak layer is a void space, with acute transitions with the adjacent strata (Figure 1.b). The SMP would record a weak (void) layer bounded by two transition zones, each the length of the sensor tip (with quadratic decreasing or increasing form) (Figure 1.b). In this example, it is clear that the actual weak layer thickness is equal to the sum of the upper transition and the apparent weak layer segment. While Birkeland et al. (2004) delineated the weak layer as the signal segment between transitions, we included both transitions to obtain the hardness maximums at the boundaries with the adjacent strata. Hence, by adding the sensor head length of 4.3 mm to the Birkeland et al. (2004) results (Figure 1.c) and subtracting the sensor head length of 4.3 mm from our separation distance (Figure 1.d), the two studies have quite comparable weak layer dimensions (12.3mm for Birkeland et al (2004) and 14.7mm and 12.4mm for this study).

5. Conclusions

The moving window statistical operations developed and employed in this study enabled stratigraphic dimension and hardness characteristics of a surface hoar weak layer to be quantified. Our main findings are that: 1) differences between the stratigraphic dimensions calculated using this and the previously used delineation technique can be accounted for, 2) the hardness of the substratum boundary possessed pronounced spatial structure which developed in a fashion consistent with recent spatial models of slope stabilization process, 3) weak layer thinning and hardening of the weak layer and its boundary with the substratum coincided with observed weak layer strengthening, 4) slab thickness positively affected the hardness of the weak layer boundaries and inversely affected its hardness variation.

Our results quantitatively support previous research that examined weak layer strengthening characteristics (Davis et al., 1996; Davis et al. 1998; Jamieson and Schweizer, 2000). An important component of this work is the application of moving window statistical operations to detect the strengthening process using the SMP. Future work will further automate this analysis technique and will utilize additional data to see if the patterns we observed repeat for other surface hoar layers. If they do, the SMP might prove to be a valuable tool for monitoring the strengthening of surface hoar weak layers.

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TABLE CAPTIONS

Table 1. Spatial statistics of SMP-derived variables at plot 1 and 2. For each variable, the best fit trend surface is listed with p- and R²-values. Variables possessing positive spatial autocorrelation have spherical semi-variogram dimensions listed. Reg. type* indicates which linear model, as defined at base of table, offered the best fit, Sig. trend signifies the presence or absence of a significant (p = 0.05) linear trend, while Pos. auto-corr. signifies the presence or absence of positive spatial auto-correlation. For both trend- and semi-variance analysis, n_{plot1} = 83, n_{plot2} = 128.

Table 2. Significant changes in slope-normal stratigraphic dimensions, including slab thickness, and the separation distance with its upper and lower segments. Mean and Median signify changes in mean and median thickness. P-value and z-score pertain to the non-parametric Mann-Whitney (Wilcoxon Rank-Sum) test (n_{plot1} = 83, n_{plot2} = 128).

Table 3. Significance of changes in SMP-derived hardness variables between Plot 1 and 2, as tested using the non-parametric Mann-Whitney (Wilcoxon Rank-Sum) test (n_{plot1} = 83, n_{plot2} = 128). Variables exhibiting significant (p-value = 0.05) changes in median values are listed in bold print. Mean signifies the change in mean hardness or the CoV of hardness.

Table 4. Regression results of correlations between slab thickness and weak layer hardness (n_{plot1} = 83, n_{plot2} = 128). Significant (p = 0.05) correlations are listed in bold.

Table 1.

Variable	Plot 1 (9 January)									Plot 2 (15 January)								
	Best fit linear trend model				Spherical semi-variogram model					Best fit linear trend model				Semi-variogram model				
	Sig. trend	Reg. type*	p-value	R ²	Pos. auto-corr.	range	partial sill	nugget	nugget sill	Sig. trend	Reg. type*	p-value	R ²	Pos. auto-corr.	range	partial sill	nugget	nugget sill
<i>Stratigraphic Dimensions</i>																		
Slab thickness (mm)	yes	1	0.044	0.049	no	—	—	—	—	yes	5	0.029	0.071	yes	2.28	284.7414	96.3788	0.25
Separation Distance (mm)	yes	2	0.001	0.122	yes	10.36	1.6662	4.2679	0.72	no	1	0.434	0.005	no	—	—	—	—
Upper segment (d') (mm)	no	3	0.831	0.001	no	—	—	—	—	no	2	0.205	0.013	no	—	—	—	—
Lower segment (d'') (mm)	yes	2	0.001	0.133	no	—	—	—	—	no	2	0.477	0.004	no	—	—	—	—
<i>Superstratum Boundary Hardness</i>																		
Max (N)	no	3	0.407	0.008	no	—	—	—	—	yes	2	0.006	0.058	yes	5.25	0.0007	0.0040	0.85
98th (N)	no	2	0.289	0.014	no	—	—	—	—	yes	2	0.003	0.068	yes	1.81	0.0024	1.0E-10	4.1E-08
90th (N)	no	2	0.215	0.019	no	—	—	—	—	yes	2	0.003	0.066	yes	1.45	0.0011	1.0E-10	9.3E-08
75th (N)	no	2	0.264	0.015	no	—	—	—	—	yes	2	0.003	0.069	yes	2.27	0.0005	0.0002	0.32
Median (N)	no	2	0.286	0.014	no	—	—	—	—	yes	2	0.003	0.067	yes	5.92	0.0001	0.0004	0.73
25th (N)	no	2	0.259	0.016	no	—	—	—	—	yes	2	0.004	0.064	yes	1.51	0.0004	1.0E-10	2.6E-07
10th (N)	no	2	0.319	0.012	no	—	—	—	—	yes	2	0.004	0.063	yes	1.52	0.0003	1.0E-10	3.5E-07
Min (N)	no	2	0.469	0.006	no	—	—	—	—	yes	5	0.001	0.124	yes	1.54	0.0002	1.0E-10	6.5E-07
CoV	no	1	0.655	0.002	no	—	—	—	—	no	2	0.558	0.003	yes	1.60	0.0046	1.0E-10	2.2E-08
<i>Upper Transition Hardness</i>																		
Max (N)	no	1	0.493	0.006	yes	6.08	0.0034	0.0018	0.34	yes	3	0.043	0.032	no	—	—	—	—
98th (N)	no	1	0.868	0.000	yes	7.50	0.0010	0.0013	0.55	yes	5	0.037	0.066	yes	1.71	0.0026	1.0E-10	3.8E-08
90th (N)	no	1	0.695	0.002	yes	2.36	0.0008	1.0E-10	1.2E-07	no	3	0.057	0.028	yes	2.19	0.0007	0.0001	0.17
75th (N)	no	1	0.581	0.004	no	—	—	—	—	yes	2	0.015	0.046	yes	4.01	0.0001	0.0002	0.63
Median (N)	no	1	0.697	0.002	no	—	—	—	—	yes	3	0.007	0.056	no	—	—	—	—
25th (N)	no	1	0.552	0.004	no	—	—	—	—	yes	3	0.003	0.067	yes	1.24	0.0001	1.0E-10	1.1E-06
10th (N)	no	1	0.498	0.006	no	—	—	—	—	yes	3	0.007	0.056	no	—	—	—	—
Min (N)	yes	2	0.037	0.052	yes	3.18	2.4E-05	2.4E-05	0.51	yes	3	0.002	0.071	no	—	—	—	—
CoV	no	1	0.658	0.002	no	—	—	—	—	no	3	0.193	0.013	yes	1.36	0.0284	0.0093	0.25
<i>Weak Layer Middle Hardness</i>																		
Max (N)	no	2	0.386	0.009	yes	5.14	0.0033	0.0010	0.24	yes	2	0.023	0.040	no	—	—	—	—
98th (N)	no	2	0.680	0.002	yes	5.05	0.0010	0.0009	0.47	yes	3	0.019	0.043	no	—	—	—	—
90th (N)	no	5	0.470	0.031	no	—	—	—	—	yes	3	0.001	0.084	no	—	—	—	—
75th (N)	no	5	0.398	0.037	no	—	—	—	—	yes	3	3.6E-04	0.097	no	—	—	—	—

Median (N)	no	5	0.411	0.036	no	—	—	—	—	yes	3	3.1E-04	0.098	no	—	—	—	—
25th (N)	no	5	0.525	0.028	no	—	—	—	—	yes	3	2.9E-04	0.099	no	—	—	—	—
10th (N)	no	5	0.424	0.035	no	—	—	—	—	yes	3	8.6E-05	0.116	no	—	—	—	—
Min (N)	no	1	0.370	0.010	no	—	—	—	—	yes	2	5.1E-06	0.153	yes	6.77	2.2E-05	2.7E-05	0.56
CoV	no	5	0.285	0.047	no	—	—	—	—	yes	3	0.005	0.062	no	—	—	—	—
Lower Transition Hardness																		
Max (N)	no	1	0.197	0.020	yes	7.59	0.0017	0.0008	0.32	yes	2	0.026	0.039	no	—	—	—	—
98th (N)	no	1	0.086	0.036	yes	6.75	0.0014	0.0003	0.19	yes	3	0.008	0.054	yes	8.54	0.0004	0.0012	0.77
90th (N)	no	1	0.077	0.038	yes	6.85	0.0010	0.0002	0.18	yes	3	0.011	0.050	yes	8.28	0.0003	0.0006	0.68
75th (N)	no	1	0.104	0.032	yes	6.78	0.0006	0.0002	0.29	yes	3	0.009	0.053	yes	5.29	0.0003	0.0003	0.53
Median (N)	no	1	0.137	0.027	no	—	—	—	—	yes	3	0.004	0.065	yes	4.47	0.0002	0.0001	0.30
25th (N)	no	1	0.227	0.018	yes	5.94	0.0001	0.0001	0.58	yes	3	0.001	0.086	yes	7.76	0.0007	0.0003	0.28
10th (N)	no	2	0.260	0.016	no	—	—	—	—	yes	3	3.4E-05	0.128	no	—	—	—	—
Min (N)	yes	2	0.025	0.060	no	—	—	—	—	yes	3	1.7E-06	0.167	yes	12.47	2.1E-05	3.4E-05	0.61
CoV	no	5	0.225	0.053	no	—	—	—	—	yes	3	0.001	0.080	yes	1.52	0.0175	0.0009	0.05
Substratum Boundary																		
Max (N)	yes	1	0.010	0.079	yes	6.08	0.0034	0.0018	0.34	yes	5	0.017	0.079	yes	8.12	0.0027	0.0023	0.47
98th (N)	yes	1	0.010	0.080	yes	6.39	0.0037	1.0E-10	2.7E-08	yes	5	0.005	0.099	yes	7.96	0.0022	0.0011	0.33
90th (N)	yes	1	0.012	0.076	yes	6.94	0.0032	1.0E-10	3.1E-08	yes	5	0.001	0.121	yes	7.93	0.0016	0.0007	0.31
75th (N)	yes	1	0.013	0.074	yes	6.92	0.0027	1.0E-10	3.7E-08	yes	5	0.001	0.124	yes	8.08	0.0014	0.0006	0.29
Median (N)	yes	1	0.015	0.070	yes	6.94	0.0022	1.0E-10	4.6E-08	yes	5	0.001	0.128	yes	7.87	0.0011	0.0003	0.22
25th (N)	yes	4	0.022	0.091	yes	7.05	0.0017	1.0E-10	5.9E-08	yes	5	0.001	0.124	yes	4.15	4.2E-05	1.9E-05	0.31
10th (N)	yes	5	0.010	0.133	yes	6.98	0.0013	1.0E-10	7.8E-08	yes	5	0.001	0.121	yes	7.84	0.0005	0.0002	0.32
Min (N)	yes	2	0.004	0.097	yes	6.67	0.0006	1.0E-10	1.6E-07	yes	5	0.001	0.131	yes	7.89	0.0003	0.0001	0.28
CoV	yes	5	0.002	0.171	yes	5.56	0.0013	0.0009	0.42	yes	5	0.007	0.093	yes	5.72	0.0022	0.0016	0.43
* Regression models: 1: $t(s) \sim x$; 2: $t(s) \sim y$; 3: $t(s) \sim x,y$; 4: $t(s) \sim x+y$; 5: $t(s) \sim x+y + x,y$, whereby ' $t(s)$ ' denotes the trend surface, ' x ' and ' y ' the cross- and up-slope coordinates, and ' x,y ' the relationship between x and y																		

Table 2.

	Separation Distance	Lower Segment of Separation Distance (d')	Upper Segment of Separation Distance (d'')	Slab thickness
Mean \pm Std. dev. _{Plot 1} [mm]	18.99 \pm 2.56	10.04 \pm 2.39	8.95 \pm 1.83	236.89 \pm 7.22
Mean \pm Std. dev. _{Plot 2} [mm]	16.69 \pm 2.10	9.20 \pm 1.81	7.49 \pm 1.90	253.19 \pm 18.10
Mean [mm]	-2.30	-0.84	-1.46	16.30
Mean [%]	-12.11	-8.41	-16.28	6.88
Median _{Plot 1} [mm]	18.96	10.24	9.04	236.89
Median _{Plot 2} [mm]	16.54	9.34	7.26	253.19
Median [mm]	-2.42	-0.91	-1.79	16.30
Median [%]	-12.76	-8.85	-19.74	6.88
p-value	<0.001	<0.001	0.002	<0.001
z-score	6.9	5.4	3.1	-7.6

Table 3.

Variable	Plot 1 Mean ± Std. dev.	Plot 2 Mean ± Std. dev.	p-value	z-score	Mean	Mean [%]
<i>Superstratum Boundary</i>						
Max (N)	0.2022 ± 0.0599	0.2027 ± 0.0723	0.881	0.2	0.0006	0.0028
98th (N)	0.1615 ± 0.0443	0.1566 ± 0.0538	0.367	0.9	-0.0049	-0.0306
90th (N)	0.1329 ± 0.0339	0.1205 ± 0.0337	0.034	2.1	-0.0124	-0.0933
75th (N)	0.1139 ± 0.0284	0.0989 ± 0.0282	0.001	3.3	-0.0150	-0.1318
Median (N)	0.0967 ± 0.0251	0.0799 ± 0.0239	<0.001	4.6	-0.0168	-0.1739
25th (N)	0.0809 ± 0.0224	0.0628 ± 0.0205	<0.001	5.5	-0.0181	-0.2238
10th (N)	0.0683 ± 0.0204	0.0500 ± 0.0177	<0.001	6.3	-0.0184	-0.2687
Min (N)	0.0381 ± 0.0161	0.0212 ± 0.0129	<0.001	7.6	-0.0169	-0.4429
CoV	0.2649 ± 0.0506	0.3551 ± 0.0690	<0.001	9.3	0.0902	0.3406
<i>Upper Transition</i>						
Max (N)	0.1751 ± 0.0692	0.1960 ± 0.0819	0.089	-1.7	0.0209	0.1192
98th (N)	0.1303 ± 0.0442	0.1360 ± 0.0559	0.87	-0.2	0.0057	0.0435
90th (N)	0.0899 ± 0.0280	0.0885 ± 0.0288	0.739	0.3	-0.0014	-0.0160
75th (N)	0.0665 ± 0.0199	0.0617 ± 0.0201	0.111	1.6	-0.0047	-0.0712
Median (N)	0.0463 ± 0.0154	0.0390 ± 0.0141	0.001	3.4	-0.0073	-0.1585
25th (N)	0.0301 ± 0.0120	0.0227 ± 0.0095	<0.001	4.6	-0.0074	-0.2465
10th (N)	0.0201 ± 0.0098	0.0133 ± 0.0077	<0.001	5.1	-0.0068	-0.3366
Min (N)	0.0003 ± 0.0072	-0.0036 ± 0.0077	<0.001	3.7	-0.0039	-13.9707
CoV	0.5813 ± 0.1649	0.7213 ± 0.1837	<0.001	5.4	0.1399	0.2407
<i>Weak Layer Middle</i>						
Max (N)	0.1267 ± 0.0580	0.1497 ± 0.0618	0.002	-3	0.0229	0.1810
98th (N)	0.0808 ± 0.0380	0.0940 ± 0.0430	0.012	-2.5	0.0131	0.1626
90th (N)	0.0444 ± 0.0202	0.0498 ± 0.0218	0.046	-2	0.0053	0.1196
75th (N)	0.0288 ± 0.0142	0.0296 ± 0.0130	0.277	-1.1	0.0009	0.0299
Median (N)	0.0182 ± 0.0104	0.0173 ± 0.0079	0.64	-0.5	-0.0008	-0.0462
25th (N)	0.0109 ± 0.0078	0.0097 ± 0.0062	0.86	0.2	-0.0012	-0.1063
10th (N)	0.0055 ± 0.0065	0.0044 ± 0.0057	0.767	0.3	-0.0011	-0.2023
Min (N)	-0.0077 ± 0.0061	-0.0094 ± 0.0071	0.234	1.2	-0.0017	0.2145
CoV	0.9030 ± 0.2499	1.0515 ± 0.4372	0.046	2	0.1485	0.1645
<i>Lower Transition</i>						
Max (N)	0.1406 ± 0.0502	0.1742 ± 0.0588	<0.001	-4.7	0.0336	0.2393
98th (N)	0.1017 ± 0.0408	0.1176 ± 0.0388	<0.001	-3.9	0.0159	0.1567
90th (N)	0.0753 ± 0.0325	0.0817 ± 0.0294	0.018	-2.4	0.0064	0.0845
75th (N)	0.0564 ± 0.0259	0.0589 ± 0.0235	0.18	-1.3	0.0025	0.0452
Median (N)	0.0390 ± 0.0195	0.0387 ± 0.0172	0.846	-0.2	-0.0002	-0.0061
25th (N)	0.0256 ± 0.0137	0.0238 ± 0.0114	0.429	0.8	-0.0018	-0.0686
10th (N)	0.0162 ± 0.0097	0.0143 ± 0.0081	0.388	0.9	-0.0020	-0.1208
Min (N)	-0.0020 ± 0.0067	-0.0038 ± 0.0078	0.152	1.4	-0.0019	0.9453
CoV	0.5725 ± 0.1055	0.6604 ± 0.1381	<0.001	4.4	0.0879	0.1535
<i>Substratum Boundary</i>						
Max (N)	0.2083 ± 0.0628	0.2357 ± 0.0644	<0.0001	-3.8	0.0275	0.1318
98th (N)	0.1677 ± 0.0552	0.1828 ± 0.0522	0.008	-2.7	0.0151	0.0901
90th (N)	0.1385 ± 0.0495	0.1473 ± 0.0454	0.088	-1.7	0.0088	0.0633
75th (N)	0.1185 ± 0.0453	0.1230 ± 0.0413	0.312	-1	0.0046	0.0385
Median (N)	0.0995 ± 0.0404	0.1003 ± 0.0363	0.801	-0.3	0.0008	0.0085
25th (N)	0.0795 ± 0.0349	0.0780 ± 0.0310	0.718	0.4	-0.0016	-0.0198
10th (N)	0.0638 ± 0.0295	0.0612 ± 0.0266	0.383	0.9	-0.0026	-0.0413
Min (N)	0.0279 ± 0.0205	0.0255 ± 0.0191	0.274	1.1	-0.0024	-0.0864
CoV	0.3047 ± 0.0489	0.3488 ± 0.0645	<0.001	5.2	0.0441	0.1448

Table 4.

Variable	Plot 1			Plot 2		
	p-value	R ²	Coeff.	p-value	R ²	Coeff.
<i>Stratigraphic Dimensions</i>						
Separation Distance (mm)	0.0299	0.0569	0.0846	0.0002	0.1088	0.0385
Upper segment (mm)	0.0377	0.0522	0.0578	0.0041	0.0646	0.0266
Lower segment (mm)	0.4677	0.0065	0.0268	0.1730	0.0149	0.0119
<i>Superstratum Boundary Hardness</i>						
Max (N)	0.0937	0.0343	0.0015	0.0053	0.0610	0.0010
98th (N)	0.0150	0.0709	0.0016	0.0006	0.0913	0.0009
90th (N)	0.0098	0.0795	0.0013	3.8E-05	0.1285	0.0007
75th (N)	0.0243	0.0610	0.0010	1.2E-05	0.1440	0.0006
Median (N)	0.0257	0.0600	0.0009	2.7E-06	0.1633	0.0005
25th (N)	0.0282	0.0581	0.0007	1.0E-06	0.1758	0.0005
10th (N)	0.0387	0.0517	0.0006	7.3E-07	0.1801	0.0004
Min (N)	0.0040	0.0978	0.0007	0.0008	0.0864	0.0002
CoV	0.5452	0.0045	-0.0005	0.0173	0.0448	-0.0008
<i>Upper Transition Hardness</i>						
Max (N)	0.3717	0.0099	0.0010	0.1599	0.0159	0.0006
98th (N)	0.1355	0.0273	0.0010	0.0319	0.0366	0.0006
90th (N)	0.0172	0.0681	0.0010	0.0227	0.0412	0.0003
75th (N)	0.1163	0.0302	0.0005	0.0039	0.0651	0.0003
Median (N)	0.2109	0.0193	0.0003	0.0013	0.0806	0.0002
25th (N)	0.1606	0.0242	0.0003	0.0009	0.0851	0.0002
10th (N)	0.1386	0.0269	0.0002	0.0026	0.0707	0.0001
Min (N)	0.0181	0.0670	0.0003	0.6652	0.0015	1.7E-05
CoV	0.9853	4.2E-06	4.7E-05	0.4367	0.0049	-0.0007
<i>Weak Layer Middle Hardness</i>						
Max (N)	0.4051	0.0086	-0.0007	0.8707	0.0002	-5.0E-05
98th (N)	0.9142	0.0001	-0.0001	0.8326	0.0004	-4.5E-05
90th (N)	0.7031	0.0018	-0.0001	0.7455	0.0009	3.5E-05
75th (N)	0.5907	0.0036	-0.0001	0.6471	0.0017	3.0E-05
Median (N)	0.6055	0.0033	-0.0001	0.4327	0.0050	3.1E-05
25th (N)	0.6716	0.0022	-0.0001	0.9696	0.0000	1.2E-06
10th (N)	0.6967	0.0019	-3.9E-05	0.5779	0.0025	-1.6E-05
Min (N)	0.3850	0.0093	-0.0001	0.0600	0.0282	-0.0001
CoV	0.9675	2.1E-05	-0.0002	0.5935	0.0023	-0.0012
<i>Lower Transition Hardness</i>						
Max (N)	0.6049	0.0033	0.0004	0.0594	0.0284	0.0005
98th (N)	0.6595	0.0024	0.0003	0.0012	0.0818	0.0006
90th (N)	0.8794	0.0003	0.0001	0.0006	0.0921	0.0005
75th (N)	0.7249	0.0015	0.0001	0.0009	0.0850	0.0004
Median (N)	0.7103	0.0017	0.0001	0.0038	0.0657	0.0002
25th (N)	0.8316	0.0006	4.5E-05	0.0283	0.0382	0.0001
10th (N)	0.9536	4.2E-05	8.7E-06	0.1092	0.0206	0.0001
Min (N)	0.8159	0.0007	2.4E-05	0.4779	0.0041	-2.7E-05
CoV	0.4232	0.0079	-0.0013	0.6626	0.0015	-0.0003
<i>Substratum Boundary Hardness</i>						
Max (N)	0.1265	0.0286	0.0015	2.6E-05	0.1336	0.0013
98th (N)	0.0667	0.0409	0.0015	1.9E-08	0.2258	0.0014
90th (N)	0.0695	0.0401	0.0014	3.4E-10	0.2733	0.0013
75th (N)	0.0787	0.0377	0.0012	6.6E-11	0.2918	0.0012
Median (N)	0.0701	0.0399	0.0011	3.6E-11	0.2987	0.0011
25th (N)	0.0761	0.0383	0.0009	1.7E-12	0.3317	0.0010
10th (N)	0.0640	0.0417	0.0008	2.0E-12	0.3303	0.0008
Min (N)	0.0375	0.0523	0.0006	1.1E-08	0.2325	0.0005
CoV	0.0344	0.0541	-0.0016	2.0E-09	0.2526	-0.0018

FIGURE CAPTIONS

Fig. 1. a) The SMP sensor head is depicted above a resistance profile of the weak layer of interest. The upper and lower transitions (circles 1 and 2) in the raw resistance values appear to be equal in length with the sensor head. The two superimposed sensor heads represent the probable location of the sensor head as it begins to enter ('p₁') and exit ('p₂') the weak layer. b) The dotted line is an approximate descriptor of a hypothetical signal, representing a conical surface area function of the percentage of the sensor head that would be in contact with homogenous super- and substrata, assuming acute transition properties. The quadratically decreasing and increasing force values are less obvious in the raw force signal in *a*), most likely due to heterogeneous nature of snow micro-structure at the transitions. c) The probable weak layer dimension based on *b*). d) Manual weak layer delineation, as conducted in previous research. e) The separation distance, examined in this study.

Fig. 2. The local coordinate system consisted of three axes: a slope-normal z-axis with origin at the snow surface was used to analyze slab and weak layer dimensions, a cross-slope x-axis and an up-slope y-axis.

Fig. 3. Sample design at plots 1 and 2. The x-axis was oriented cross-slope and the y-axis up-slope.

Fig. 4. Five of the statistical profiles generated from the SMP resistance signal (grey) at profile 10 in plot 2. These statistical profiles represent the minimum, the 10th percentile, the median (Q2), the 90th percentile and the maximum of the SMP signal encountered at the scale of the sensor head.

Fig. 5. The five defined stratigraphic positions within and adjacent to the weak layer are superimposed on a median profile from a SMP profile at plot 2.

Fig. 6. Empirical and spherical modeled semivariograms of the median hardness of the substratum boundary at plots 1 and 2 (semivariance analysis utilized the following sample sizes: $n_{\text{plot1}} = 83$, $n_{\text{plot2}} = 128$). Between plots 1 and 2, the changes in model dimensions (increase in range, decrease in partial sill and increase in nugget) were evident in nearly all hardness variables at the substratum boundary.

Fig. 7. Boxplots of selected variables showing significant changes between 9 and 15 January, including a) the separation distance between the super- and substrata boundaries, b) the slab thickness, and c) the size-corrected shear strength index. Black circles = median, box ends = 1st and 3rd quartiles, whiskers = 1.5 * inter-quartile range, white circles = outliers.

Fig. 8. Graphical summary of the changes in weak layer hardness, as described by non-parametric statistics. Significant (p 0.05) changes in hardness are shown on plot 2, whereby +/- signs are used to describe significant increases or decreases in hardness.

Fig. 9. Plot summaries of statistical profiles.

Fig. 10. At both plots the coefficient of variation (CoV) was greatest within the weak layer and smallest at the boundaries with the adjacent strata. Numbers indicate stratigraphic positions while arrows indicate relative change of CoV and stratigraphic position, relative to the substratum boundary position.

FIGURES

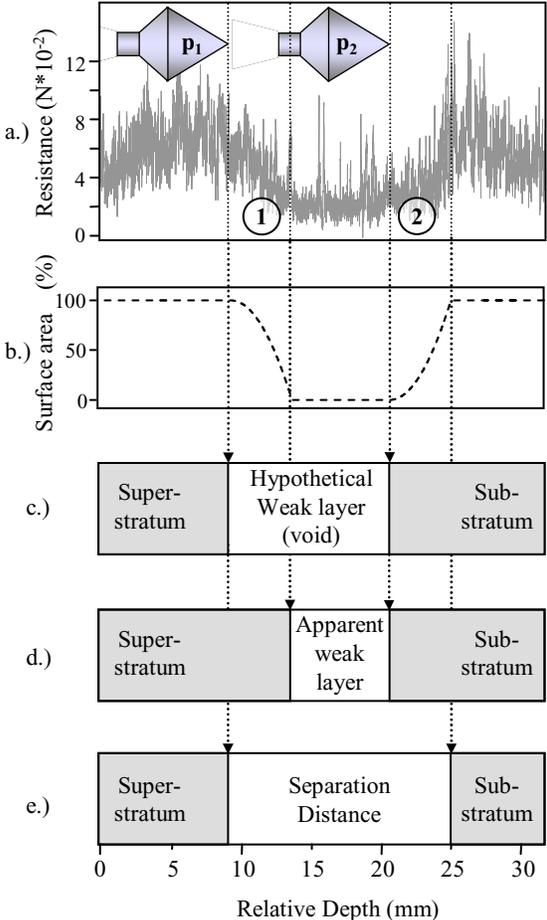


Fig. 1.

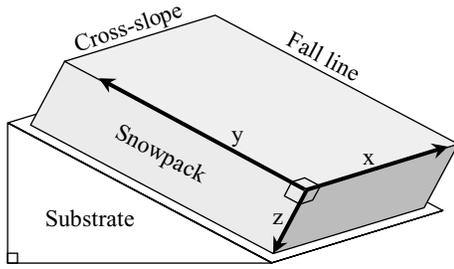


Fig. 2.

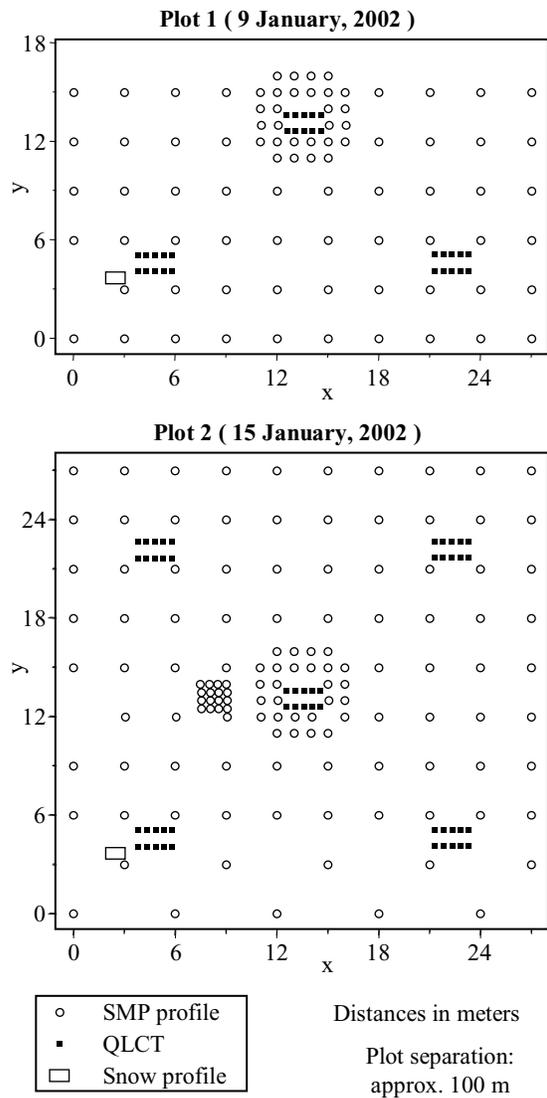


Fig. 3.

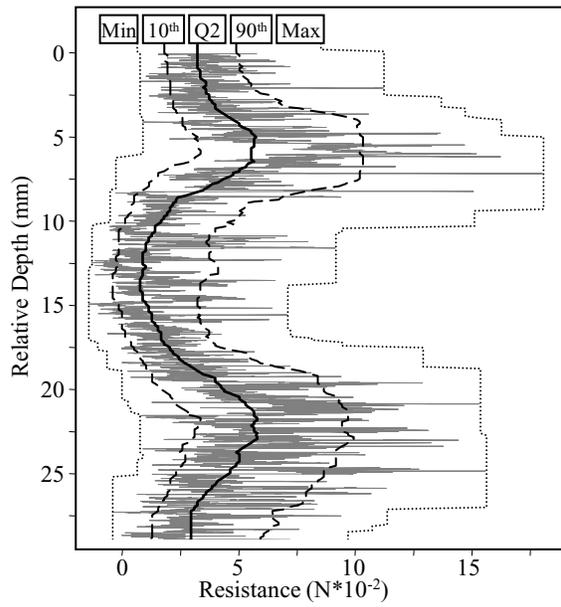


Fig. 4.

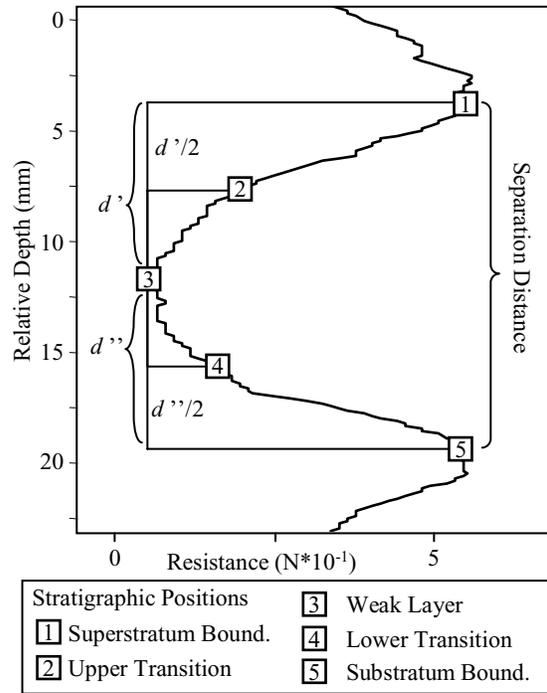


Fig. 5.

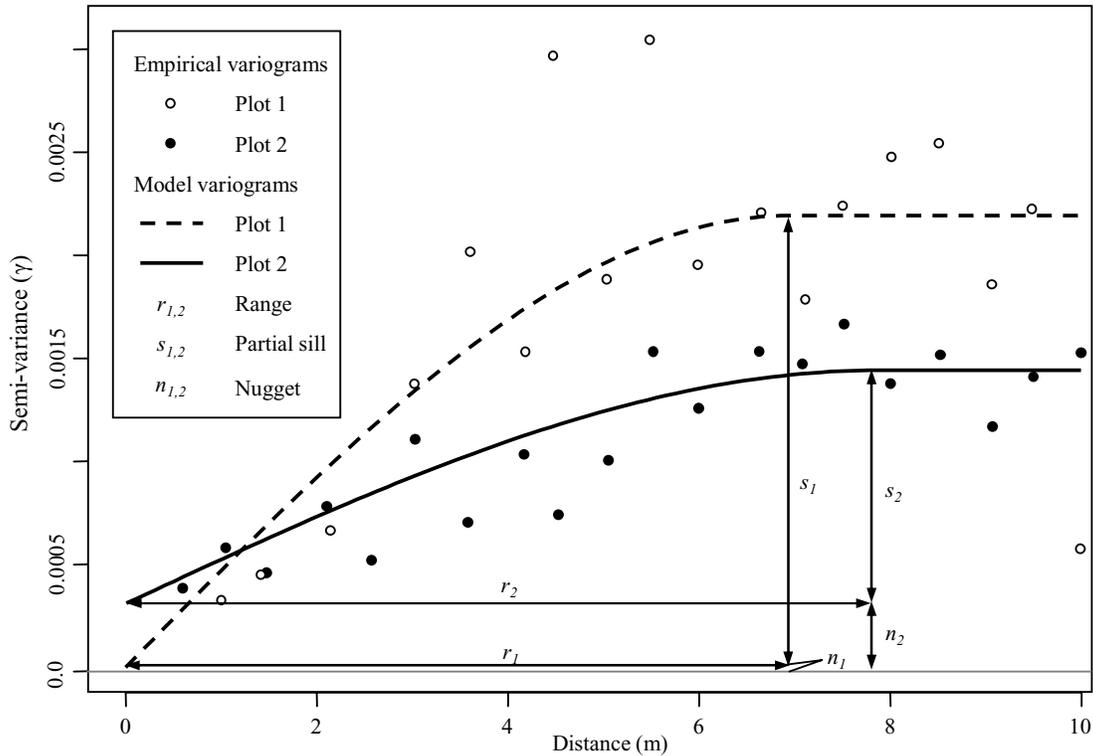


Fig. 6.

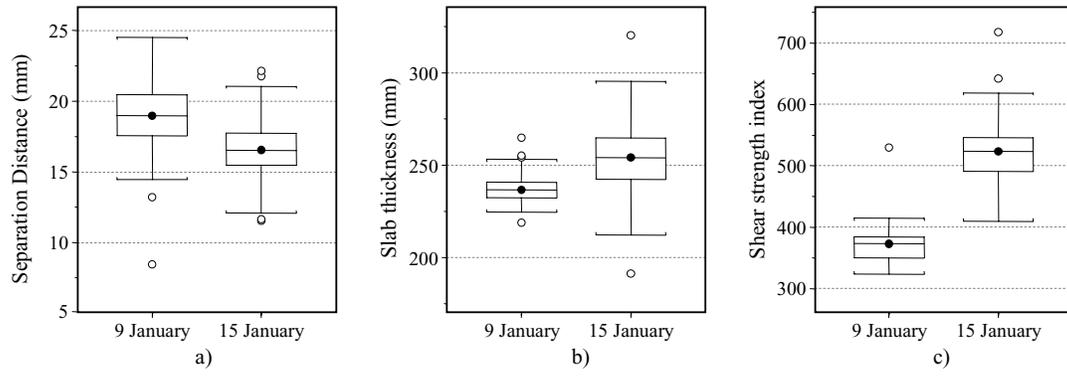


Fig. 7.

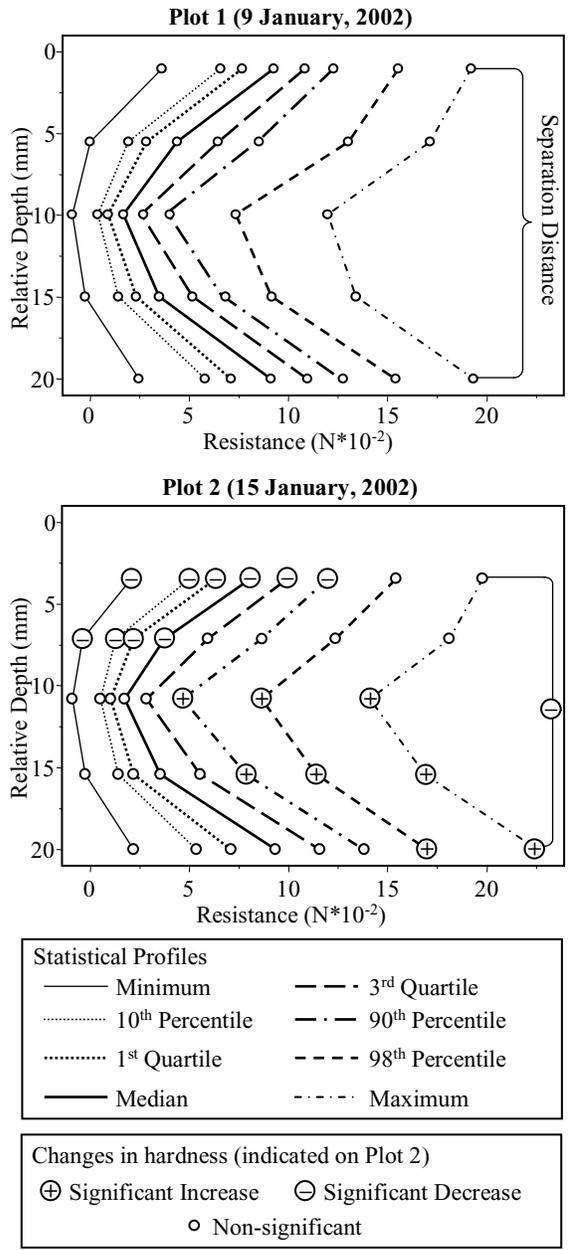


Fig. 8.

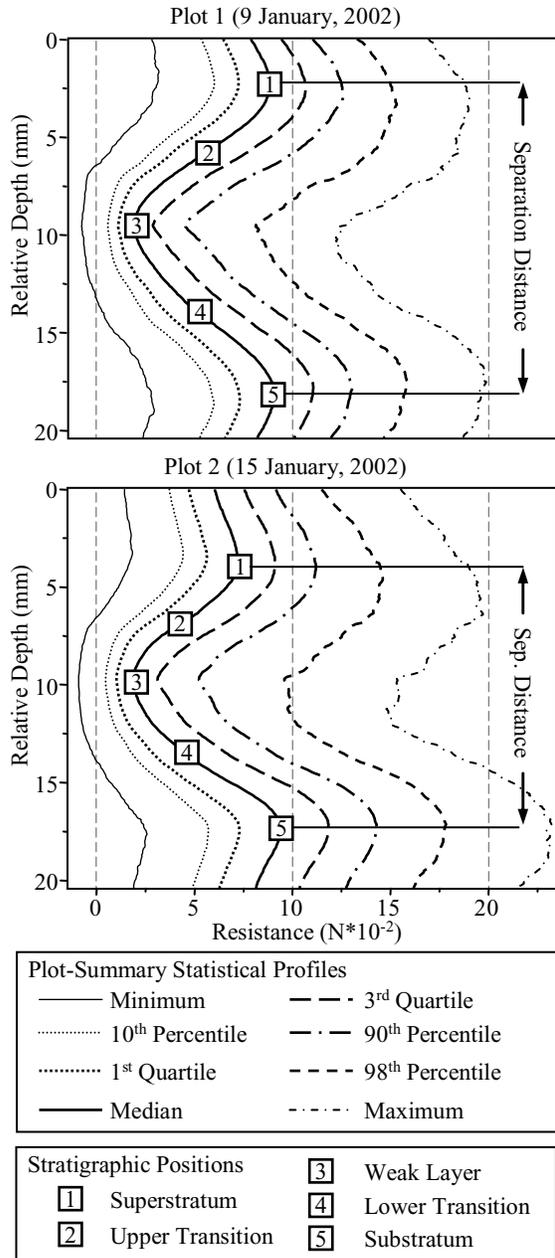


Fig. 9.

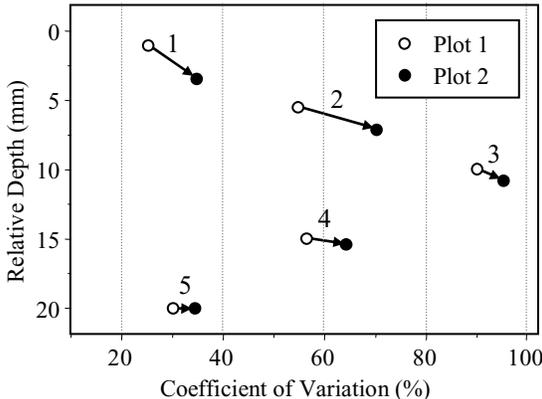


Fig. 10.